Carnegie Mellon University

Tree Indexes – Part



Intro to Database Systems

Andy Pavlo Computer Science Carnegie Mellon University

ADMINISTRIVIA

Project #1 is due Sunday Sept 27th

Homework #2 is due Sunday Oct 4th





UPCOMING DATABASE TALKS

CockroachDB Query Optimizer

 \rightarrow Monday Sept 28th @ 5pm ET



Apache Arrow

 \rightarrow Monday Oct 5th @ 5pm ET

DataBricks Query Optimizer \rightarrow Monday Oct 12th @ 5pm ET



Sector Secto



DATA STRUCTURES

Internal Meta-data Core Data Storage **Temporary Data Structures**

Table Indexes





TABLE INDEXES

A <u>table index</u> is a replica of a subset of a table's attributes that are organized and/or sorted for efficient access using a subset of those attributes.

The DBMS ensures that the contents of the table and the index are logically in sync.



TABLE INDEXES

It is the DBMS's job to figure out the best index(es) to use to execute each query.

There is a trade-off on the number of indexes to create per database.

- \rightarrow Storage Overhead
- \rightarrow Maintenance Overhead



TODAY'S AGENDA

B+Tree Overview Using B+Trees in a DBMS





B-TREE FAMILY

There is a specific data structure called a **<u>B-Tree</u>**.

People also use the term to generally refer to a class of balanced tree data structures:

- \rightarrow **B-Tree** (1971)
- → **B+Tree** (1973)
- → **B*Tree** (1977?)
- $\rightarrow B^{link}$ -Tree (1981)



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15-445/645 (Fall 2020) \rightarrow **B**^{link}-**Tree** (1981)

Efficient Locking for Concurrent Operations

PHILIP L. LEHMAN Carnegie-Mellon University and S. BING YAO Purdue University

The B-tree and its variants have been found to be highly useful (both theoretically and in practice) The D-tree and us variance new open round to us many userus toost incorrections and as partners, for storing large amounts of information, especially on secondary storage devices. We examine the for scoung sage smouths or automation, especially on secondary bounge or vices. The standard way problem of overcoming the inherent difficulty of concurrent operations on such structures, using a process os overcomença que emereten tambanty os constartens operationa on such taratcutera, emag a practical storage model. A single additional "link" pointer in each node allows a process to easily presentes storage modifications performed by other concurrent processes. Our solution compares recover nom use monuncations performed by other tons from processes out sension comparison favorably with earlier solutions in that the locking scheme is simpler (no read-locks are used) and involancy with earlier solutions in that the needing externs is support the requirements are used, and only a (small) constant number of nodes are locked by any update process at any given time. An Key Words and Phrases: database, data structures, B-tree, index organizations, concurrent algorithms,

concurrency controls, locking protocols, correctness, consistency, multiway search trees CR Categories: 3.73, 3.74, 4.32, 4.33, 4.34, 5.24

1. INTRODUCTION

The B-tree [2] and its variants have been widely used in recent years as a data structure for storing large files of information, especially on secondary storage devices [7]. The guaranteed small (average) search, insertion, and deletion time for these structures makes them quite appealing for database applications.

A topic of current interest in database design is the construction of databases

that can be manipulated concurrently and correctly by several processes. In this paper, we consider a simple variant of the B-tree (actually of the B*-tree, proposed by Wedekind [15]) especially well suited for use in a concurrent database

Methods for concurrent operations on B*-trees have been discussed by Bayer and Schkolnick [3] and others [6, 12, 13]. The solution given in the current paper

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Authors' present addresses: P. L. Lehman, Department of Computer Science, Carnegie Mellon Automa presents doutremest. F. & Letonman, Department of Computer Science, Outremestations, University, Pittaburgh, PA 15213; S. B. Yao, Department of Computer Science and College of Business and Management, University of Maryland, College Park, MD 20742. © 1981 ACM 0362-5915/81/1200-0650 \$00.75 ACM Transactions on Database Systems, Vol. 6, No. 4, December 1981, Pages 650-670.

B-TREE FAMILY

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B+TREE

- A **B**+**Tree** is a self-balancing tree data structure that keeps data sorted and allows searches, sequential access, insertions, and deletions in O(log n).
- \rightarrow Generalization of a binary search tree in that a node can have more than two children.
- \rightarrow Optimized for systems that read and write large blocks of data.

15-445/645 (Fall 2020)

The Ubiguitous B-Tree

DOUGLAS COMER

Computer Science Department, Purdue University, West Lafayette, Indiana 47907

B-trees have become, de facto, a standard for file organization. File indexes of users, dedicated database systems, and general-purpose access methods have all been proposed and implemented using B-trees This paper reviews B-trees and shows why they have been so successful It discusses the major variations of the B-tree, especially the B+-tree, contrasting the relative merits and costs of each implementation. It illustrates a general purpose access method which uses a B-tree.

Keywords and Phrases: B-tree, B*-tree, B*-tree, file organization, index

CR Categories: 3.73 3.74 4.33 4 34

INTRODUCTION

The secondary storage facilities available on large computer systems allow users to store, update, and recall data from large collections of information called files. A computer must retrieve an item and place it in main memory before it can be processed. In order to make good use of the computer resources, one must organize files intelligently, making the retrieval process efficient.

The choice of a good file organization depends on the kinds of retrieval to be performed. There are two broad classes of retrieval commands which can be illustrated by the following examples:

Sequential: "From our employee file, prepare a list of all employees' names and addresses," and

"From our employee file, ex- to the employee file, where the topmost Random: tract the information about index consists of labels on drawers, and the employee J. Smith".

We can imagine a filing cabinet with three folders. drawers of folders, one folder for each em-

next level of index consists of labels on Natural hierarchies, like the one formed ployee. The drawers might be labeled "A- by considering last names as index entries, G," "H-R," and "S-Z," while the folders do not always produce the best perform-

might be labeled with the employees' last names. A sequential request requires the

searcher to examine the entire file, one folder at a time. On the other hand, a

random request implies that the searcher,

guided by the labels on the drawers and

cessed file in a computer system is an index

which, like the labels on the drawers and

folders of the file cabinet, speeds retrieval

by directing the searcher to the small part of the file containing the desired item. Fig-

ure 1 depicts a file and its index. An index

may be physically integrated with the file,

like the labels on employee folders, or phys-

ically separate, like the labels on the drawers. Usually the index itself is a file. If the

index file is large, another index may be

built on top of it to speed retrieval further,

and so on. The resulting hierarchy is similar

folders, need only extract one folder. Associated with a large, randomly ac-

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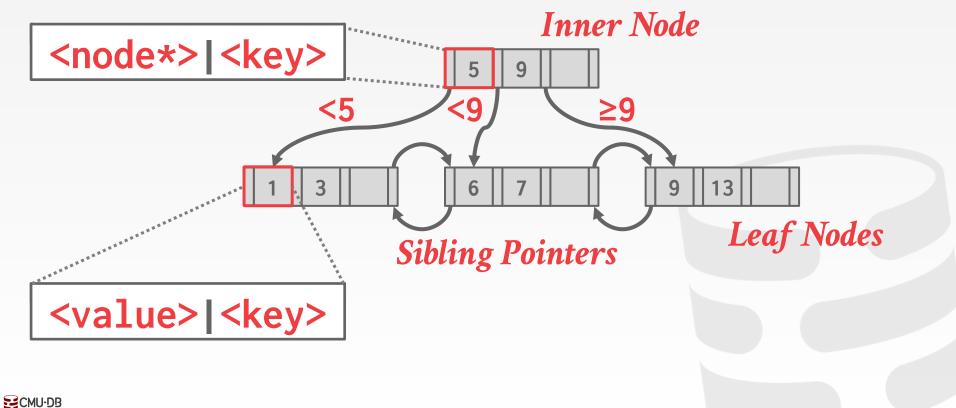
Computing Surveys, Vol. 11, No. 2, June 1979

B+TREE PROPERTIES

A B+Tree is an *M*-way search tree with the following properties:

- \rightarrow It is perfectly balanced (i.e., every leaf node is at the same depth in tree).
- → Every node other than the root, is at least half-full
 M/2-1 ≤ #keys ≤ M-1
- \rightarrow Every inner node with k keys has k+1 non-null children

B+TREE EXAMPLE



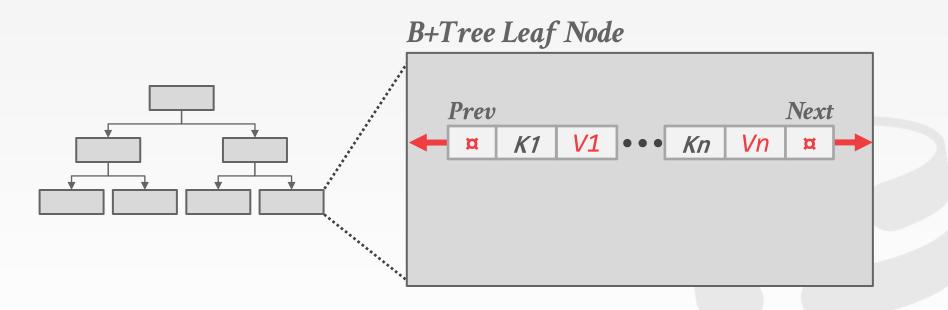
NODES

Every B+Tree node is comprised of an array of key/value pairs.

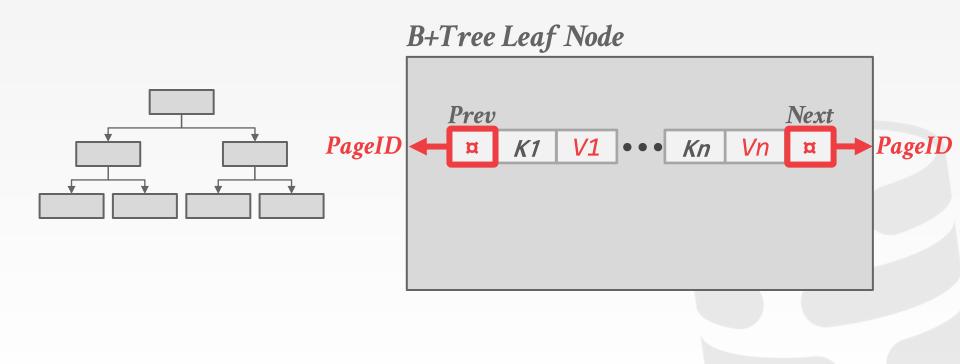
- \rightarrow The keys are derived from the attributes(s) that the index is based on.
- \rightarrow The values will differ based on whether the node is classified as <u>inner nodes</u> or <u>leaf nodes</u>.

The arrays are (usually) kept in sorted key order.

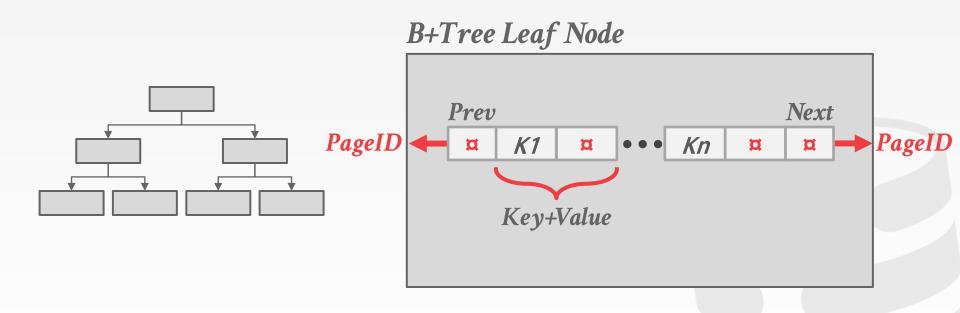






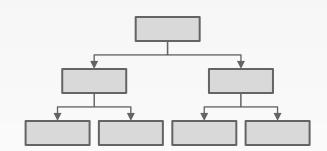


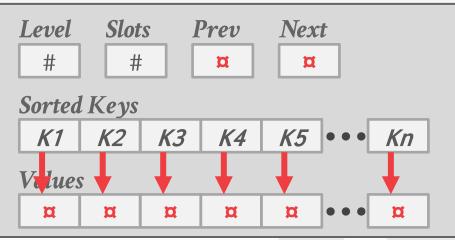






B+Tree Leaf Node







LEAF NODE VALUES

Approach #1: Record Ids

 \rightarrow A pointer to the location of the tuple that the index entry corresponds to.

Approach #2: Tuple Data

- \rightarrow The actual contents of the tuple is stored in the leaf node.
- \rightarrow Secondary indexes must store the record id as their values.



PostgreSQL Server



B-TREE VS. B+TREE

The original **B-Tree** from 1972 stored keys + values in all nodes in the tree.

 \rightarrow More space efficient since each key only appears once in the tree.

A **B+Tree** only stores values in leaf nodes. Inner nodes only guide the search process.



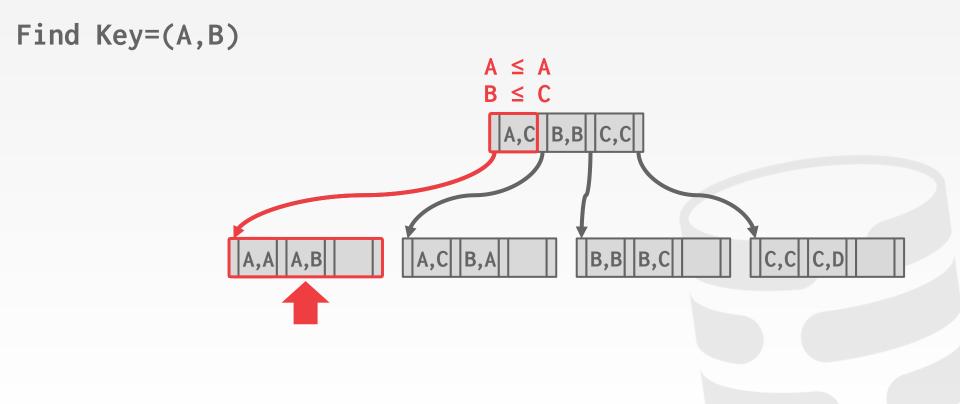
The DBMS can use a B+Tree index if the query provides any of the attributes of the search key.

Example: Index on <a,b,c>

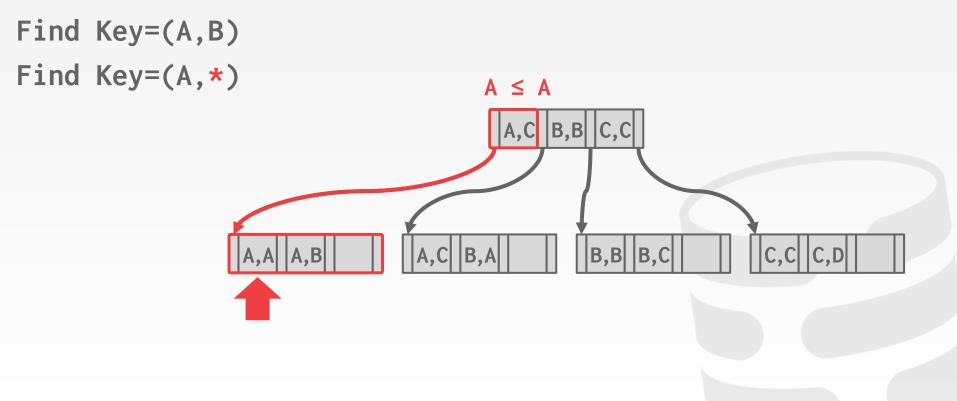
- \rightarrow Supported: (a=5 AND b=3)
- \rightarrow Supported: (b=3).

Not all DBMSs support this.

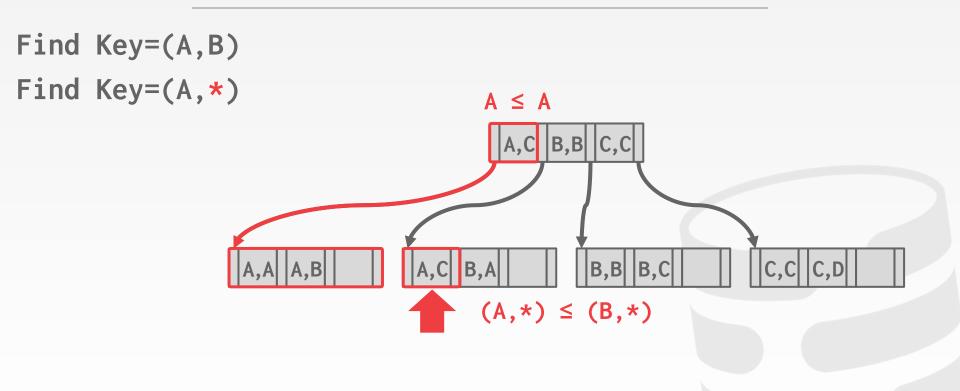
For hash index, we must have all attributes in search key.



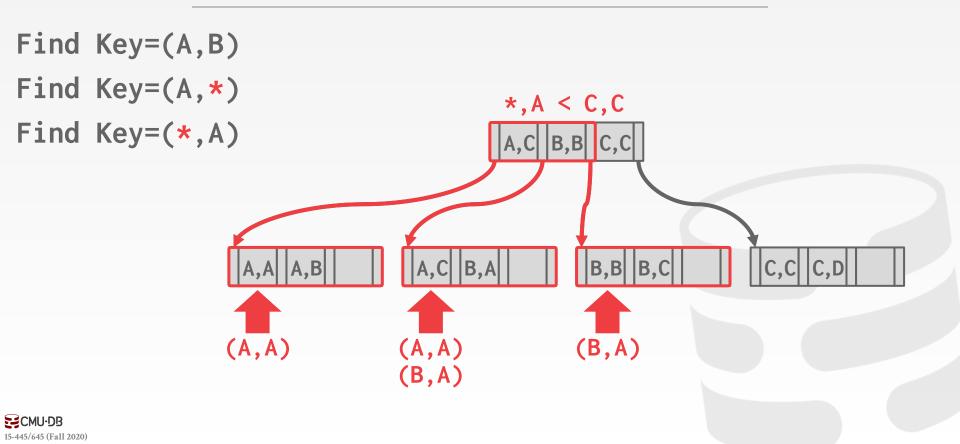












B+TREE - INSERT

Find correct leaf node L. Put data entry into L in sorted order. If L has enough space, done! Otherwise, split L keys into L and a new node L2 \rightarrow Redistribute entries evenly, copy up middle key. \rightarrow Insert index entry pointing to L2 into parent of L.

To split inner node, redistribute entries evenly, but push up middle key.

Source: <u>Chris Re</u> **CMU-DB** 15-445/645 (Fall 2020)

B+TREE VISUALIZATION

https://cmudb.io/btree

Source: David Gales (Univ. of San Francisco)



B+TREE - DELETE

Start at root, find leaf L where entry belongs. Remove the entry.

- If L is at least half-full, done!
- If L has only M/2-1 entries,
- \rightarrow Try to re-distribute, borrowing from sibling (adjacent node with same parent as L).
- \rightarrow If re-distribution fails, merge L and sibling.

If merge occurred, must delete entry (pointing to L or sibling) from parent of L.

Source: <u>Chris Re</u> **CMU-DB** 15-445/645 (Fall 2020)

B+TREE - DUPLICATE KEYS

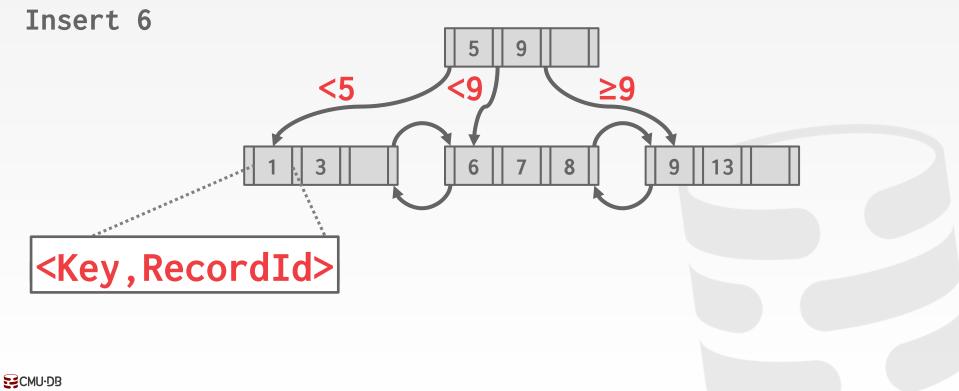
Approach #1: Append Record Id

- \rightarrow Add the tuple's unique record id as part of the key to ensure that all keys are unique.
- \rightarrow The DBMS can still use partial keys to find tuples.

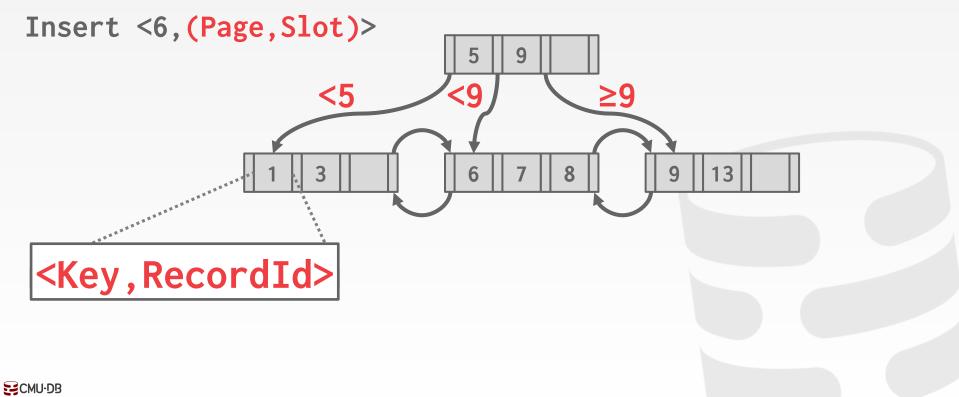
Approach #2: Overflow Leaf Nodes

- \rightarrow Allow leaf nodes to spill into overflow nodes that contain the duplicate keys.
- \rightarrow This is more complex to maintain and modify.

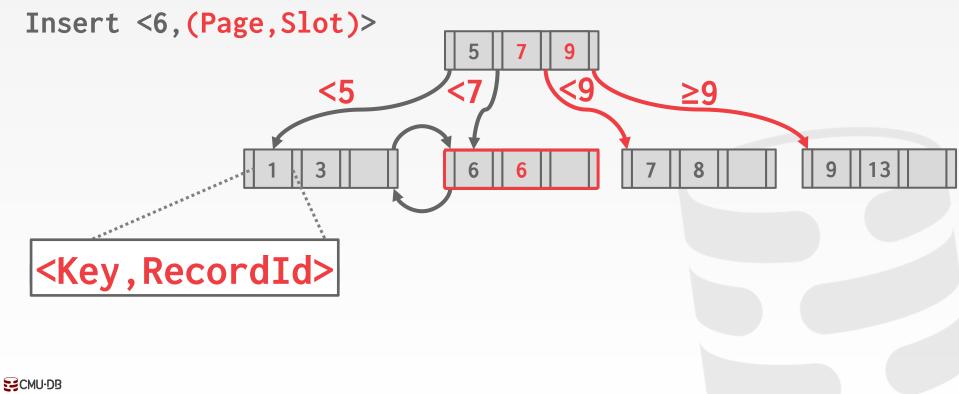
B+TREE - APPEND RECORD ID



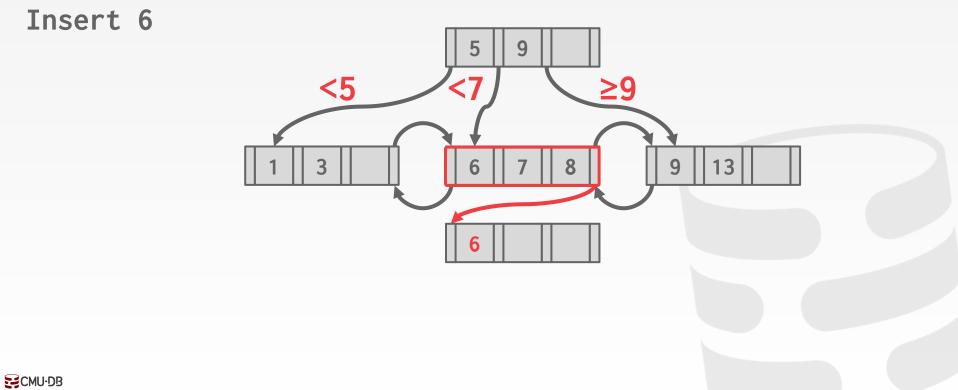
B+TREE - APPEND RECORD ID



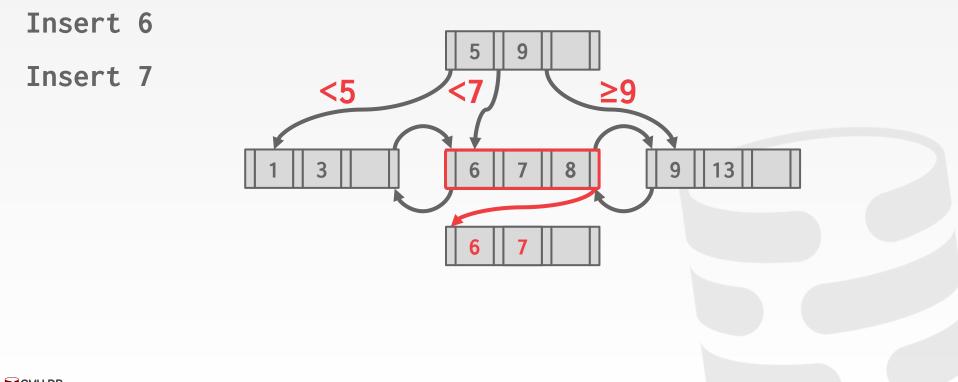
B+TREE - APPEND RECORD ID



B+TREE - OVERFLOW LEAF NODES

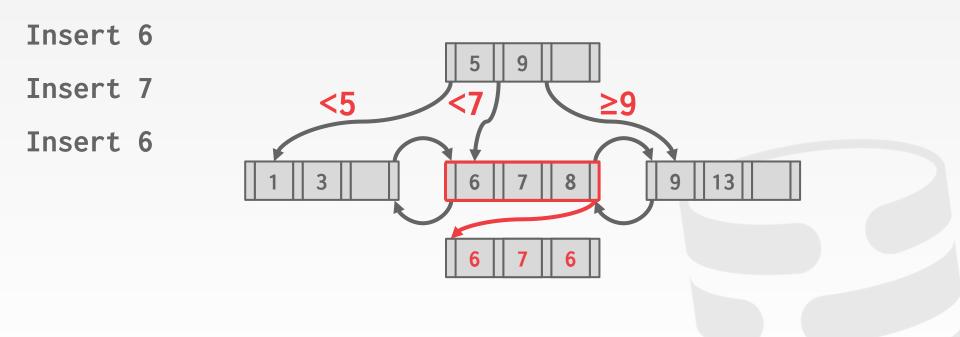


B+TREE - OVERFLOW LEAF NODES





B+TREE - OVERFLOW LEAF NODES





CLUSTERED INDEXES

The table is stored in the sort order specified by the primary key.

 \rightarrow Can be either heap- or index-organized storage.

Some DBMSs always use a clustered index.

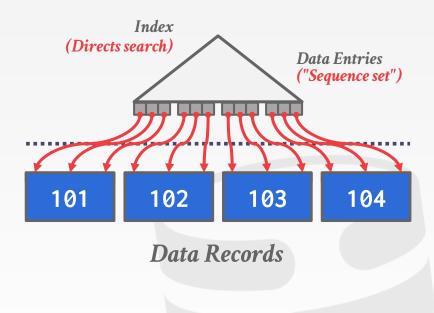
 \rightarrow If a table does not contain a primary key, the DBMS will automatically make a hidden row id primary key.

Other DBMSs cannot use them at all.

CLUSTERED B+TREE

Traverse to the left-most leaf page, and then retrieve tuples from all leaf pages.

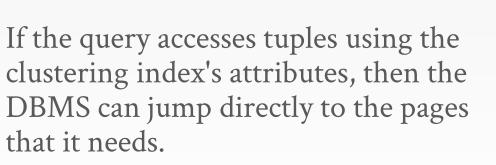
This will always better than external sorting.





HEAP CLUSTERING

Tuples are sorted in the heap's pages using the order specified by a <u>clustering index</u>.



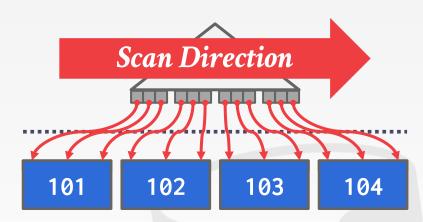




HEAP CLUSTERING

Tuples are sorted in the heap's pages using the order specified by a <u>clustering index</u>.

If the query accesses tuples using the clustering index's attributes, then the DBMS can jump directly to the pages that it needs.



INDEX SCAN PAGE SORTING

Retrieving tuples in the order that appear in an unclustered index is inefficient.

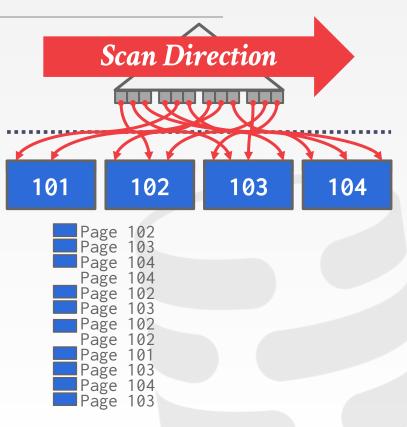
The DBMS can first figure out all the tuples that it needs and then sort them based on their page id.



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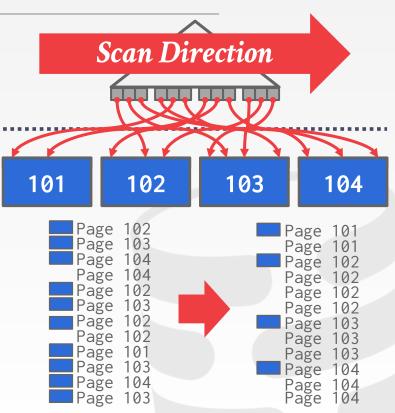




INDEX SCAN PAGE SORTING

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DEMO

B+Tree vs. Hash Indexes Table Clustering





CONCLUSION

The venerable B+Tree is always a good choice for your DBMS.





NEXT CLASS

More B+Trees Tries / Radix Trees Inverted Indexes

