# Iterators, Relational Operators and Joins <br> Hash Join Algorithms 

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Reading: R \& G Chapter 12 \& 14

## Naïve in Memory Hash Join: R $\bowtie$ S

What if $R$ doesn't fit?

- Requires equality predicate:
- Works for Equi-Joins \& Natural Joins
- Assume R is smaller relation
- Require R to fit in memory
- Simple algorithm:
- Load all R into hash table
- Scan S and probe R
- Memory requirements?

- $[R]$ < (B-2) * hash_fill_factor


## Properties that help

- $\sigma_{\text {sid }=4 \vee \text { sid }=6}\left(R \bowtie_{\text {sid }} S\right)=\sigma_{\text {sid }=4}\left(R \bowtie_{\text {sid }} S\right) \cup \sigma_{\text {sid }=6}\left(R \bowtie_{\text {sid }} S\right)$
- Can Decompose Into Smaller "Partial Joins"
- $R \bowtie_{\text {sid }} S=U\left(\sigma_{\text {hash(sid) }}(R) \bowtie_{\text {sid }} \sigma_{\text {hash(sid) }}(S)\right)$
- Pick a hash function so that each $\sigma_{\text {hash(sid) }}(R)$ fits in memory!


## Announcements

- Midterm next week!
- Review session tomorrow
- Include descriptions in your OH tickets
- Try out "party" mode and let us know how it goes
- Please turn on your video if you can


## Grace Hash Join

- Requires equality predicate:
- Equi-Joins \& Natural Joins


University of Tokyo's GRACE

- Two Stages:
- Partition tuples from R and $S$ by join key and store on scratch disk
- all tuples for a given key now reside in same partition
- same partition might have tuples with different keys but same hash value
- Build \& Probe a separate hash table for each partition (like in Naïve Hash)
- Assume partition of smaller relation fits in memory
- Recurse if necessary...


## Remember External Hashing?

Hash partitions hp of
size $\sim N /(B-1)$


Hash partitions hr Fully hashed!

## Sketch of Grace Hash Join



Hash partitions hr Fully hashed!

## Sketch of Grace Hash Join, cont.



## PsuedoCode, Grace Hash

```
For Cur in {R, S}
    For page in Cur
        Read page into input buffer
        For tup on page
            Place tup in output buf hash(tup.joinkey)
            If output buf full then flush to disk partition
    Flush output bufs to disk partitions
```



## PsuedoCode, Grace Hash, cont.

```
For Cur in {R, S}
    For page in Cur
    Read page into input buffer
    For tup on page
            Place tup in output buf hash(tup.joinkey)
            If output buf full then flush to disk partition
    Flush output bufs to disk partitions
For i in [0..(B-1)) // for each partition
    For page in R }\mp@subsup{R}{i}{
    For tup on page
        Build tup into memory hash(tup.joinkey)
    For page in Si
    Read page into input buffer
    For tup on page
        Probe memory hash(tup.joinkey) for matches
        Send all matches to output buffer
        Flush output buffer if full
```


## Grace Hash Join

- An animation
- Two phases:
- Partition (divide)
- Build \& Probe hash tables (conquer)


## Grace Hash Join: Partition




B-1 Buffers


## Grace Hash Join: Partition, Part 2



## Grace Hash Join: Partition, Part 3



## Grace Hash Join: Partition Part 4



## Grace Hash Join: Partition Part 5



B-1 Buffers



## Grace Hash Join: Partition Part 6




B-1 Buffers


## Grace Hash Join: Partition Part 7



B-1 Buffers



## Grace Hash Join: Partition Part 8




## Grace Hash Join: Partition 9



## Grace Hash Join: Partition Part 10



Grace Hash Join: Partition Part 11


## Grace Hash Join: Partition Part 12

- Each key is assigned to one partition - e.g., green star keys only in Partition 1
- Sensitive to key Skew
- Purple circle key
- Each partition could be on a different disk or even different machine



## Grace Hash Join: Build \& Probe



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 2



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 3



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 4



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 5



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 6



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 7



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 8



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 9



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 10



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 11



Blue tuples are from $R$
Orange tuples are from $S$

## Grace Hash Join: Build \& Probe Part 12



Blue tuples are from $R$
Orange tuples are from $S$

## Summary of Grace Hash Join



## What is the Cost?

## Cost of Hash Join

$$
\begin{aligned}
& {[R]=1000, p_{R}=100,|R|=100,000} \\
& {[S]=500, p_{S}=80,|S|=40,000}
\end{aligned}
$$



- Partitioning phase: read+write both relations
$\Rightarrow 2([\mathrm{R}]+[\mathrm{S}]) \mathrm{I} / \mathrm{Os}$
- Matching phase: read both relations, forward output
$\Rightarrow[\mathrm{R}]+[\mathrm{S}]$
- Total cost of 2-pass hash join $=3([\mathrm{R}]+[\mathrm{S}])$
- 3 * $(1000+500)=4500$


## Cost of Hash Join Part 2



- What's the max size of $R$ that can be processed in 1 pass of build \& probe?
- Build hash table on R with uniform partitioning
- Partitioning Phase divides R into (B-1) runs of size [R]/ (B-1)
- Matching Phase requires each ([R]/(B-1)) < (B-2)
- Solving backwards gives $\mathrm{R}<(\mathrm{B}-1)(\mathrm{B}-2) \approx \mathrm{B}^{2}$
- Note: no constraint on size of S (probing relation)!


## Cost of Hash Join Part 3

$$
[R]=1000, p_{R}=100,|R|=100,000
$$



- Naïve Hash Join: requires [R] < B
- Put all of R in hash table
- $1 / 3$ the I/O cost of Grace!


## TINSTAFL!!

- Grace Hash Join: 2-passes for $[R]<B^{2}$
- Hybrid Hash Join: an algorithm that adapts between the two
- Tricky to tune


## Hash Join vs. Sort-Merge Join

- Sorting pros:
- Good if input already sorted, or need output sorted
- Not sensitive to data skew or bad hash functions
- Hashing pros:
- For join: \# passes depends on size of smaller relation
- E.g. if smaller relation is $<\mathrm{B}$, naïve/hybrid hashing is great
- Good if input already hashed, or need output hashed


## Recap

- Nested Loops Join
- Works for arbitrary $\Theta$
- Make sure to utilize memory in blocks
- Index Nested Loops
- For equi-joins
- When you already have an index on one side
- Sort/Hash
- For equi-joins
- No index required
- Hash better if one relation is much smaller than other
- No clear winners - may want to implement them all
- Be sure you know the cost model for each
- You will need it for query optimization!

